



# MODULATIONAL INSTABILITY OF ION-ACOUSTIC WAVE IN PLASMAS WITH TWO ELECTRON TEMPERATURE DISTRIBUTION

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## ABSTRACT

The modulation instability of ion-acoustic waves has been theoretically investigated in an unmagnetized collisionless plasma with (hot and cold) electrons, positrons and ions. A nonlinear Schrödinger equation (NLSE) has been derived by using the KBM method. The positron concentration, temperature ratio of the ion to electron, cold electron concentration, temperature ratio of cold to hot electrons and positron temperature are shown to play significant role in the modulation instability of ion-acoustic waves.

**Key words:** ion acoustic wave, nonlinear Schrödinger equation, , KBM method, modulational instability.

## I. INTRODUCTION

During the last few years electron-positron-ion (EPI) plasmas attracted attention due to their importance both in laboratory experiments and in space plasma observations [1-3]. Electron-positron plasmas are found in astrophysical plasmas such as magnetosphere of pulsars, in active galactic nuclei, in early universe, and in the regions of the accretion disks surrounding the central black holes [4-6]. Therefore, the study of electron-positron-ion (EPI) plasmas is important to understand the behavior of both astrophysical [1-3,7-9] and laboratory plasmas [10-12]. In the last two decades there has been a great deal of interest in the study of nonlinear wave phenomena in both unmagnetized and magnetized EPI plasmas [13-21].

Several authors have derived the nonlinear Schrödinger equation by either using the reductive perturbation method [22-23] or the Krylov Bogoliubov Mitropolsky (KBM) method [24] have studied the stability of ion-acoustic waves against modulational instability in a collisionless plasma consisting of cold ions and hot electrons. It has been shown [24] that the ion-acoustic waves are modulationally unstable for wave numbers greater than a normalized critical wave number  $k_c$  ( $= 1.47$ ). The modulational instability of ion acoustic wave with warm ions have been studied using reductive perturbation method [27] and KBM method [25] in unmagnetized electron ion plasmas. The modulational instability of ion acoustic wave with negative ions in



plasmas have been investigated by Mishra et al. [26] The modulational instability of ion acoustic waves in plasmas with superthermal electrons have been studied by Gharaee et al. [28]

The modulation instability of electrostatic modes in both EPI as well as in pair plasmas has been a subject of great interest in the recent years [29-30]. The nonlinear amplitude modulation of low-frequency electrostatic ion waves propagating in collisionless magnetized EPI plasma are studied [31]. Zhang et al. [32] have investigated modulation instability of ion-acoustic waves in electron-positron-ion plasma with nonthermally distributed electrons and cold ions. Eslami et al. [33] have studied modulation instability of ion-acoustic waves in electron-positron-ion plasma with electrons and positrons following q-nonextensive distribution. The nonlinear amplitude modulation of ion-acoustic wave in the presence of warm ions in unmagnetized EPI plasmas [34]. However, in the course of their study, they have taken the same temperature for the electron and positron species. Therefore, their analysis cannot be used to study the modulational instability of ion-acoustic waves in EPI plasmas in which electron and positron species are at different temperatures. A nonlinear Schrödinger equation which describes the modulational instability of ion-acoustic soliton is derived by using the multiple scale method, the dispersive and nonlinear coefficients are obtained which is depend upon the temperature of the ions, concentration of the positrons, electrons and dust particles [35]. Chawla et al. [20] studied the modulational instability of ion-acoustic waves in EPI. Modulational instability of ion-acoustic waves has been theoretically investigated [36] in an unmagnetized collisionless plasma with nonthermal electrons, Boltzmann positrons, and warm positive ions.

The modulational instability of ion-acoustic waves in a two-electron temperature plasma has been studied by Sharma and Buti [37] for parallel modulation. They found that due to the presence of cold electron component, the critical wave number for modulational instability reduces, which increases the unstable region in k-space. It has also been shown by them that the unstable region ( in k-space ) significantly depends upon the relative densities and temperatures of two electron components. The modulational instability of obliquely modulated ion-acoustic waves in two-electron-temperature collisionless plasma has been investigated by Yashvir et al. [38]. Their study reveals that there exists a wide domain in the  $(k - \phi)$  plane in which the large amplitude ion-acoustic waves would be modulationally unstable. Chhabra and Sharma [39] studied the nonlinear oblique modulation of ion-acoustic waves in a two warm ion plasma. Mishra et al. [40] studied the modulational instability of obliquely modulated ion-acoustic waves in a collisional plasma with one and two electron temperature distributions. The modulational instability of obliquely modulated ion-acoustic waves in a collisionless plasma consisting of two-ion species with different masses, concentrations, and charge states have been studied by Mishra et al. [41]. In that analysis, the ion species were taken as cold. Nonlinear modulation of ion-acoustic waves in two-electron-temperature plasmas studied by Esfandyari-kalejahi et al. [42]. Existence and characteristics of ion-acoustic wave modulation are studies [43] in a plasma with two-temperature electron satisfying kappa distribution.

The paper has been organized as follows: In Section II, the normalized fluid equations for the system have been presented. The nonlinear Schrödinger equation has been derived in Sec. III and in Sec. IV, stability analysis has been discussed. The conclusions are summarized in Sec. V.

## II. BASIC EQUATIONS

We consider a plasma consisting of warm adiabatic ions and isothermal electrons, which are divided into two groups: a hot component with density  $n_h$  and temperature  $T_h$  and a cold component with density  $n_c$  and temperature  $T_c$ . The nonlinear behavior of ion-acoustic waves may be described by the following set of normalized fluid equations:

$$\frac{\partial n}{\partial t} + \frac{\partial}{\partial x}(nv) = 0 \tag{1}$$

$$\frac{\partial v}{\partial t} + v \frac{\partial v}{\partial x} = E - \sigma n \nabla n \tag{2}$$

$$\nabla n_h = -\frac{\beta}{(\mu + \nu\beta)} n_h E \tag{3}$$

$$\nabla n_c = -\frac{1}{(\mu + \nu\beta)} n_c E \tag{4}$$

$$\nabla n_p = \gamma n_p E \tag{5}$$

$$\nabla \cdot E = (1 - \alpha)n + \alpha n_p - n_h - n_c \tag{6}$$

where

$$\alpha = \frac{n_p^{(0)}}{n^{(0)}}, \quad \mu = \frac{n_c^{(0)}}{n^{(0)}}, \quad \nu = \frac{n_h^{(0)}}{n^{(0)}}, \quad \beta = \frac{T_c}{T_h}, \quad \gamma = T_p / T_e, \quad \text{and} \quad \sigma = 3T_i / T_e$$

In the above equations,  $n$  and  $v$  are the density and fluid velocity of the ion species,  $E$  is the electric field,  $n_h$  is the hot electron density,  $n_c$  is the cold electron density and  $n_p$  is the positron density.  $\sigma = 3T_i / T_e$ , defines the temperature ratio of adiabatic warm ions to electrons of the plasma and  $\gamma = T_p / T_e$ , the ratio temperature of positron with electron fluid. We have normalized the quantities  $n, v, n_h, n_c, n_p, x, E$  and  $t$  with

$$n_0, C_s = (kT_e / e), \quad \lambda_D = \left( \frac{\epsilon_0 k T_e}{n_0 e^2} \right)^{1/2} \quad \text{and} \quad \omega_{pi}^{-1} \quad \text{respectively.}$$

## III. DERIVATION OF THE NONLINEAR SCHRÖDINGER EQUATION

Using the KBM perturbation method for nonlinear wave modulational, we expand all the quantities around the equilibrium state as follows:

$$E = \epsilon E_1 + \epsilon^2 E_2 + \epsilon^3 E_3 + \dots$$

$$v = \epsilon v_1 + \epsilon^2 v_2 + \epsilon^3 v_3 + \dots$$

$$n = 1 + \epsilon n_1 + \epsilon^2 n_2 + \epsilon^3 n_3 + \dots$$

$$\begin{aligned}
 n_h &= v + \varepsilon n_{h1} + \varepsilon^2 n_{h2} + \varepsilon^3 n_{h3} + \dots \\
 n_c &= \mu + \varepsilon n_{c1} + \varepsilon^2 n_{c2} + \varepsilon^3 n_{c3} + \dots \\
 n_p &= 1 + \varepsilon n_{p1} + \varepsilon^2 n_{p2} + \varepsilon^3 n_{p3} + \dots
 \end{aligned}
 \tag{7}$$

In order to consider the modulational instability of ion-acoustic waves in the system, we assume that the perturbed quantities of all orders depend on x and t through the complex amplitudes ( a ,  $\bar{a}$  ) and phase factor (  $\psi$  ). The phase factor is given by

$$\psi = kx - \omega t
 \tag{8}$$

The complex amplitude a is a slowly varying function of x and t expressed as

$$\frac{\partial a}{\partial t} = \varepsilon A_1(a, \bar{a}) + \varepsilon^2 A_2(a, \bar{a}) + \varepsilon^3 A_3(a, \bar{a}) + \dots
 \tag{9a}$$

$$\frac{\partial a}{\partial x} = \varepsilon B_1(a, \bar{a}) + \varepsilon^2 B_2(a, \bar{a}) + \varepsilon^3 B_3(a, \bar{a}) + \dots
 \tag{9b}$$

together with the complex conjugate relations to Eq. (9). The unknown functions  $A_1, A_2, \dots$  and  $B_1, B_2, \dots$  are determined so as to eliminate all secular terms in the perturbation solution.

On substituting the expression (7) into the set of equations (1) - (6), using (9) and equating terms with the same power of  $\varepsilon$ , we obtain a set of equations for each order in  $\varepsilon$ . From the first - order equations, the first order solutions are given as

$$\begin{aligned}
 n_1 &= a \exp(i\psi) + \bar{a} \exp(-i\psi) \\
 E_1 &= \frac{i}{k} \left[ (\sigma k^2 - \omega^2) \{ a \exp(i\psi) - \bar{a} \exp(-i\psi) \} \right] \\
 v_1 &= \frac{\omega}{k} [ a \exp(i\psi) + \bar{a} \exp(-i\psi) ] \\
 n_{h1} &= \left( \frac{\omega^2 - \sigma k^2}{k^2} \right) \frac{\beta v}{(\mu + \nu \beta)} [ a \exp(i\psi) + \bar{a} \exp(-i\psi) ] \\
 n_{c1} &= \left( \frac{\omega^2 - \sigma k^2}{k^2} \right) \frac{\mu}{(\mu + \nu \beta)} [ a \exp(i\psi) + \bar{a} \exp(-i\psi) ] \\
 n_{p1} &= \frac{\gamma}{k} \left[ (\sigma k^2 - \omega^2) \{ a \exp(i\psi) + \bar{a} \exp(i\psi) \} \right]
 \end{aligned}
 \tag{10}$$

The condition for these solutions to be non - trivial is obtained in the form of linear dispersion relation

$$\omega^2 = \frac{k^2(1 - \alpha)}{(1 + k^2 + \alpha \gamma)} + \sigma k^2
 \tag{11}$$

In order to get the nonsecular solution up to third order in  $\varepsilon$ , we set the constant and the coefficient of the resonant secular terms equal to zero, which gives the nonlinear Schrodinger equation:



$$i \frac{\partial a}{\partial \tau} + P \frac{\partial^2 a}{\partial \xi^2} + Q|a|^2 a = 0 \tag{12}$$

where  $\xi = \varepsilon(x - v_g t)$ ,  $\tau = \varepsilon^2 t$  (13)

$$v_g = \frac{\omega \left[ 2k^4 \sigma + k^2(1 - \alpha) + 2\sigma k^2(\alpha\gamma + 1) - \alpha\gamma k(\sigma k^2 - \omega^2) - (\sigma k^2 - \omega^2) + k^2(\sigma k^2 - \omega^2) \right]}{k \left[ \sigma k^4 + k^2 \omega^2 + k^2(1 - \alpha) + (\alpha\gamma + 1)(\sigma k^2 + \omega^2) \right]} \tag{14}$$

$$P = \frac{1}{2} \frac{dv_g}{dk}$$

$$= \frac{\left[ \begin{aligned} &[-\omega^2 \{ -3\sigma k^4 + \sigma k^2(\alpha\gamma + 1) - \alpha\gamma k(\sigma k^2 - \omega^2) + (\omega^2 - \sigma k^2) \}] \\ &- v_g \omega k \{ k^2(\sigma k^2 + \omega^2) + 2\sigma k^4 + k^2(1 - \alpha) + 2\sigma k^2(\alpha\gamma + 1) - (\alpha\gamma + 1)(\sigma k^2 + \omega^2) \} \\ &+ v_g^2 k^4 \{ \sigma k^2 + (1 - \alpha) + \sigma(\alpha\gamma + 1) \} ] / [ \omega k^2 \{ \sigma k^4 + k^2 \omega^2 + k^2(1 - \alpha) + (\sigma k^2 + \omega^2)(\alpha\gamma + 1) \} ] \right]}{\tag{15}} \end{aligned}$$

$$Q = - \left[ \begin{aligned} &\left\{ \frac{\sigma k^4 + k^2 \omega^2 + k^2(1 - \alpha) + \omega^2(\alpha\gamma + 1) + \sigma k^2(\alpha\gamma + 1)}{k^2 \omega} \right\} \{ \alpha_1 + \gamma_1 \} \\ &+ \left\{ -i \frac{(\sigma k^2 - \omega^2)}{k^4} (k\alpha\gamma^2 - 1) \right\} \{ \alpha_2 + \gamma_2 \} + \left\{ \frac{2\sigma k^2 + (1 - \alpha) + 2\sigma(\alpha\gamma + 1)}{k} \right\} \{ \alpha_3 + \gamma_3 \} \\ &+ \left\{ \frac{\alpha\gamma}{k^3} (\sigma k^2 - \omega^2) \right\} \{ -\alpha_4 + \gamma_4 \} + \left\{ \frac{(\sigma k^2 - \omega^2)}{k^3} \right\} \{ -\alpha_5 + \gamma_5 \} \\ &+ \left\{ \frac{(\sigma k^2 - \omega^2)}{k^3} \right\} \{ -\alpha_6 + \gamma_6 \} \end{aligned} \right] \times \frac{1}{\left[ \frac{\omega}{k} + \frac{\sigma k}{\omega} + \frac{(1 - \alpha)}{k\omega} + \frac{\omega(\alpha\gamma + 1)}{k^3} + \frac{\sigma k(\alpha\gamma + 1)}{k^2 \omega} \right]} \tag{16}$$

$$\alpha_1 = \frac{\omega A}{6k(\omega^2 - \sigma k^2)} \tag{17}$$

$$\alpha_2 = i \left[ 2\alpha_1 \frac{(\sigma k^2 - \omega^2)}{\omega} + 2\sigma k + \frac{(\sigma k^2 + \omega^2)}{k} \right] \tag{18}$$

$$\alpha_3 = \frac{(\alpha_1 k + \omega)}{\omega} \tag{19}$$

$$\alpha_4 = -i \frac{\alpha_2 \gamma}{2k} + \frac{\gamma^2 (\sigma k^2 - \omega^2)^2}{2k^3} \tag{20}$$

$$\alpha_5 = i \frac{\beta v}{(\mu + v\beta)} \frac{\alpha_2}{2k} + \frac{\beta^2 v}{(\mu + v\beta)^2} \frac{(\sigma k^2 - \omega^2)^2}{2k^4} \tag{21}$$

$$\alpha_6 = i \frac{\mu}{(\mu + \nu\beta)} \frac{\alpha_2}{2k} + \frac{\mu}{(\mu + \nu\beta)^2} \frac{(\sigma k^2 - \omega^2)^2}{2k^4} \tag{22}$$

$$b_2 = \left[ i \frac{(\sigma k^2 - \omega^2)}{\omega} b_1(a, \bar{a}) + \frac{(\sigma k^2 + \omega^2)}{k\omega} A_1 + 2\sigma B_1 \right] \tag{23}$$

$$b_3 = \left[ \frac{k}{\omega} b_1(a, \bar{a}) - i \frac{A_1}{\omega} - i \frac{B_1}{k} \right] \tag{24}$$

$$b_4 = \left[ -i \frac{\gamma}{k} b_2(a, \bar{a}) + i \frac{\gamma(\sigma k^2 - \omega^2)}{k^2} B_1 \right] \tag{25}$$

$$b_5 = \left[ i \frac{\beta\nu}{(\mu + \nu\beta)} \frac{1}{k} b_2(a, \bar{a}) + i \frac{\beta\nu}{(\mu + \nu\beta)} \frac{B_1}{k^3} (\omega^2 - \sigma k^2) \right] \tag{26}$$

$$b_6 = \left[ i \frac{\mu}{(\mu + \nu\beta)} \frac{1}{k} b_2(a, \bar{a}) + i \frac{\mu}{(\mu + \nu\beta)} \frac{B_1}{k^3} (\omega^2 - \sigma k^2) \right] \tag{27}$$

$$\gamma_1 = \nu_g \gamma_3 - 2 \frac{\omega}{k} a\bar{a} + c_1 \tag{28}$$

$$\gamma_2(a, \bar{a}) = 0 \tag{29}$$

$$\gamma_3 = \frac{\left[ \frac{(\sigma k^2 - \omega^2)}{k^4} (k\alpha\gamma^2 - 1) + \left\{ 2\nu_g \frac{\omega}{k} + \frac{\omega^2}{k^2} + \sigma \right\} (\alpha\gamma + 1) \right]}{\left[ \nu_g^2 (1 + \alpha\gamma) - \sigma (1 + \alpha\gamma) - (1 - \alpha) \right]} a\bar{a} + c_3 \tag{30}$$

$$\gamma_4 = (-\nu_g^2 + \sigma) \gamma_3 + \left[ \frac{\gamma^2}{k^3} (\sigma k^2 - \omega^2)^2 + \frac{\gamma\omega^2}{k^2} + \sigma\gamma + 2\nu_g \gamma \frac{\omega}{k} \right] a\bar{a} + c_4 \tag{31}$$

$$\gamma_5 = \left( \nu_g \gamma_1 - \sigma \gamma_3 \right) \left( \frac{\beta\nu}{(\mu + \nu\beta)} \right) + \left[ \frac{\beta^2\nu}{(\mu + \nu\beta)^2} \frac{(\sigma k^2 - \omega^2)^2}{k^4} - \frac{\beta\nu}{(\mu + \nu\beta)} \frac{\omega^2}{k^2} - \sigma \frac{\beta\nu}{(\mu + \nu\beta)} \right] a\bar{a} + c_5 \tag{32}$$

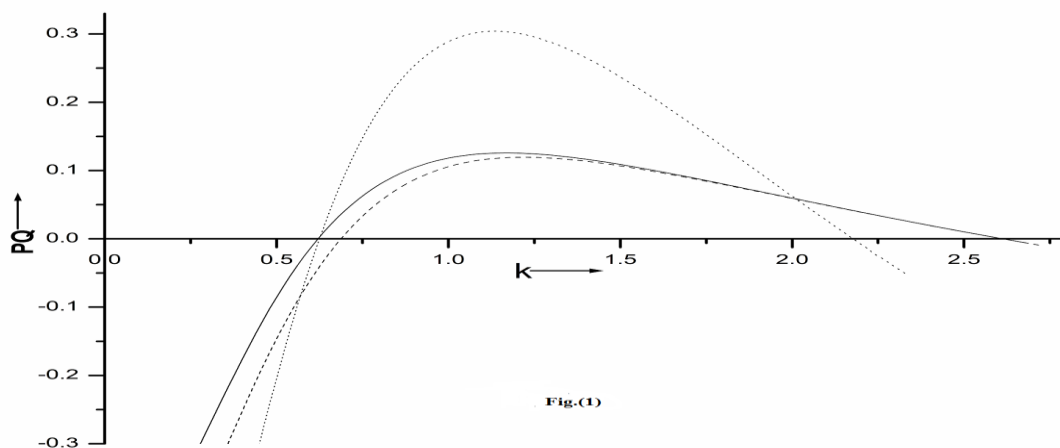
$$\gamma_6 = \left( \nu_g \gamma_1 - \sigma \gamma_3 \right) \left( \frac{\mu}{(\mu + \nu\beta)} \right) + \left[ \frac{\mu}{(\mu + \nu\beta)^2} \frac{(\sigma k^2 - \omega^2)^2}{k^4} - \frac{\mu}{(\mu + \nu\beta)} \frac{\omega^2}{k^2} - \sigma \frac{\mu}{(\mu + \nu\beta)} \right] a\bar{a} + c_6 \tag{33}$$

Here  $\gamma_2, \gamma_3, \gamma_4$  and  $\gamma_5$  are function of  $a$  and  $\bar{a}$  only and are assumed to real. Where  $c_1, c_3, c_4$ , and  $c_5$  are arbitrary constants independents of  $a, \bar{a}$  and  $\psi$  can be determined by the initial conditions. The dispersion coefficients P and the nonlinear coefficient Q are given, respectively, by equations (15) and (16).

IV. STABILITY ANALYSIS AND DISCUSSION

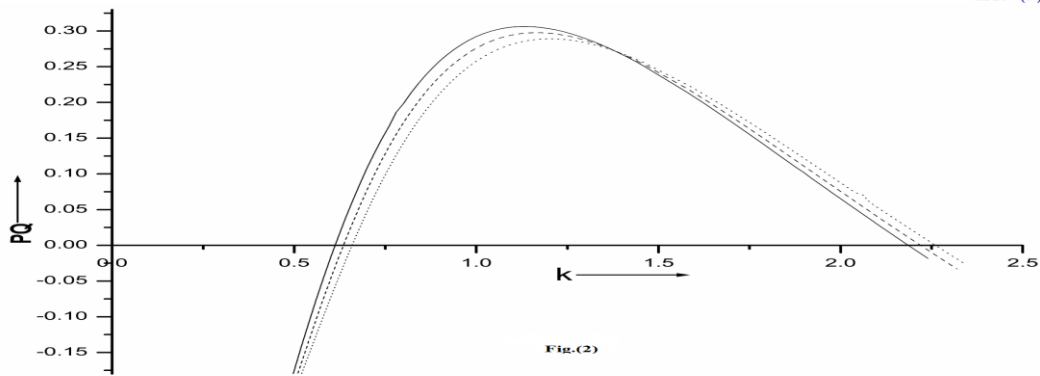
It is well known that the modulation instability depends on the sign of the product of the dispersive and nonlinear coefficient, i.e.,  $PQ$ . It is found that the presence of positron modifies the unstable region of the ion-acoustic waves which is defined by  $PQ > 0$  and the stable region of the ion-acoustic waves which is defined by  $PQ < 0$ . We have investigated that ion-acoustic waves are modulationally unstable in the range of wave numbers lying between  $k_{min} < k < k_{max}$ , where the values of  $k_{min}$  and  $k_{max}$  depends upon the cold electron concentration, temperature ratio of cold to hot electrons, ion temperature, positron concentration, and positron temperature of the plasma. For the case of cold ions and in the absence of positron, and cold electron concentration, we find the critical wave number  $k_c = 1.47$ .

Fig. 1, is a  $PQ$  versus wave number  $k$  plot for different values of temperature ratio of cold to hot electrons ( $\beta$ ) keeping the values of ion temperature ( $T_i/T_e$ ), positron concentration ( $\alpha$ ), cold electron concentration ( $\mu$ ), and positron temperature ( $\gamma$ ) constant. It shows that as the temperature ratio of cold to hot electrons ( $\beta$ ) increases, the value of  $k_{max}$  decreases.



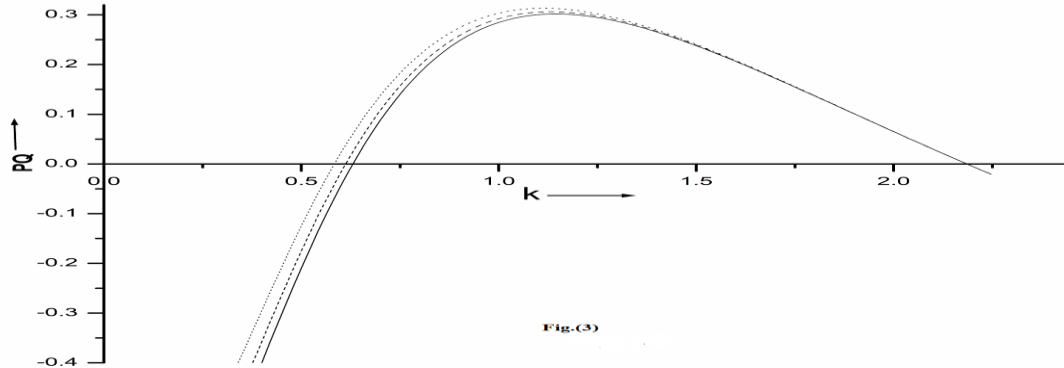
**Fig. 1** Variation of the product  $PQ$  with wave number  $k$  with  $\gamma = 0$ ,  $T_i/T_e = 0.1$ ,  $\mu = 0$ , and  $\alpha = 0$  at different values of cold to hot electron temperature ( $\beta$ ) = 0.6 (dotted line), 0.8 (dashed line) and 1 (solid line).

In Fig. 2, we have plotted the variation of  $PQ$  with respect to wave number  $k$  for different values of positron concentration ( $\alpha$ ), at ion temperature ( $T_i/T_e$ ), cold electron concentration ( $\mu$ ), temperature ratio of cold to hot electrons ( $\beta$ ), and positron temperature ( $\gamma$ ). We also note from the figure that as the positron concentration ( $\alpha$ ) increases, the values of  $k_{max}$  and  $k_{min}$  increases.



**Fig. 2** Variation of the product PQ with wave number k with  $\mu = 0.1$ ,  $T_i/T_e = 0.1$ ,  $\beta = 0.8$ , and  $\gamma = 0.8$  at different values of positron concentration ( $\alpha$ ) = 0.01 (solid line), 0.05 (dashed line) and 0.1 (dotted line).

In Fig. 3, PQ is plotted as function of k for different values of temperature ratio of cold to hot electrons ( $\beta$ ), taking other plasma parameters such as cold electron concentration ( $\mu$ ), positron concentration ( $\alpha$ ), ion temperature ( $T_i/T_e$ ), and positron temperature ( $\gamma$ ) as constant. It is seen that as the temperature ratio of cold to hot electrons ( $\beta$ ) increases, the value of  $k_{min}$  increases.



**Fig. 3** Variation of the product PQ with wave number k with  $T_i/T_e = 0.1$ ,  $\gamma = 0.8$ ,  $\mu = 0.1$ , and  $\alpha = 0.01$  at different values of cold to hot electron temperature ( $\beta$ ) = 0.6 (dotted line), 0.8 (dashed line) and 1 (solid line).

### V. CONCLUSIONS

To conclude, we have studied the modulational instability of ion acoustic waves in unmagnetized electron-positron-ion plasmas with two electron temperature distributions by employing KBM perturbation method. It is found that as the ion temperature increases, the value of  $k_{max}$  and  $k_{min}$  decreases, at the same time the region of instability also decreases. The presence of positron concentration, positron temperature ratio, temperature ratio





of cold to hot electrons and cold electron concentration, the value of  $k_{\max}$  and  $k_{\min}$  increases. For a given set of parameters values with temperature ratio of cold to hot electrons, cold electron concentration, ion temperature and positron concentration, by increasing the value of positron temperature ratio, the value of  $k_{\max}$  and  $k_{\min}$  increases. For a given set of parameters values with temperature ratio of cold to hot electrons, cold electron concentration, ion temperature and positron temperature ratio, by increasing the value of positron concentration, the value of  $k_{\max}$  and  $k_{\min}$  also increases.

In the absence of positron, temperature ratio of cold to hot electrons and increasing the value of the cold electron concentration, the value of  $k_{\min}$  increases at warm ion case. In the presence of positron, temperature ratio of cold to hot electrons and increasing the value of the cold electron concentration, the value of  $k_{\max}$  increases and  $k_{\min}$  decreases in warm ion case.

In the absence of positron, cold electron concentration and increasing the value of the temperature ratio of cold to hot electrons, the value of  $k_{\max}$  decreases at warm ion case. In the presence of positron, cold electron concentration and increasing the value of the temperature ratio of cold to hot electrons, the value of  $k_{\min}$  increases at warm ion case.

Our findings are general and may be applicable to explain the stable and unstable modulational of ion acoustic wave in astrophysical plasma situations such as neutron stars or pulsars where unmagnetized electron-positron-ion plasma with warm ions may exist.

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