Curvelet Transform and Adaboost Technique for HSI Feature Extraction

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ABSTRACT
Generally, Spectral component extraction methods are connected to the HSI information shape straightforwardly. This paper shows a novel calculation for HSI include extraction by abusing the curvelet transformed space by means of a moderately new unearthly component preparing procedure—solitary range examination (SSA). Utilizing the support vector machine classifier, trial comes about have demonstrated that elements separated by SSA on curvelet coefficients have better execution regarding grouping precision over components removed on wavelet coefficients. Since the proposed approach primarily depends on SSA for include extraction on the ghastly measurement, it really has a place with the ghastly element extraction classification. Subsequently, the proposed strategy has likewise been contrasted and some cutting edge otherworldly element extraction procedures to demonstrate its viability. Furthermore, adaboost technique is used for classification and denoising of images. By which we can obtain good feature extraction of images.

Keywords: HSI, SVM, Curvelet Transform, Single Spectrum Analysis

I. INTRODUCTION
Hyperspectral imaging (HSI) provides data with a high-resolution spectrum over 2-D images, leading to powerful capabilities related to classification in many applications, such as remote sensing. The wide range covered by the spectral information, from visible light to near infrared, allows the recognition of small differential characteristics of the content in a scene. For that reason, new emerging laboratory-based data analysis, including food quality, medical, or verification of counterfeit goods and documents [1]–[4], is based on HSI. The use of the support vector machine (SVM) as a classifier for HSI applications has been shown to be robust and highly accurate [5]–[7]. The samples or pixels are evaluated in SVM by means of their respective features or spectral bands, which can contribute to more robust discrimination as they include information from different spectral wavelengths. However, HSI data are usually prone to noise, which can reduce the discrimination ability limiting the accuracy in classification tasks. For that reason, there is great interest for a potential decomposition of the spectral profiles into components in such a way that noise could be removed or mitigated by avoiding particular components with high noisy content. In this decomposition context, a particularly interesting research area is the use of the empirical mode decomposition (EMD) technique applied in 1-D to the spectral profile of the pixels as briefly evaluated in [8]. The EMD is the main part of the Hilbert–Huang transform, an algorithm for the analysis of nonlinear and nonstationary time series [9], [10]. EMD
decomposes a 1-D signal into a few components called intrinsic mode functions (IMFs) and has been widely used in processing signal applications such as speech recognition [11]. Hence, our aim is to introduce the singular spectrum analysis (SSA) technique in a similar way to evaluate its performance for classification tasks in HSI. In this paper, we are also aiming at combining ideas of feature extraction and denoising together for improving classification accuracy of remote sensing hyperspectral images. Finally, Adaboost technique is applied inorder to increase the rate of accuracy.

II. CURVELET TRANSFORM:
For multi-scale object representation, Curvelets are a non-adaptive technique. Being an extension of the wavelet concept, they are becoming popular in similar fields of scientific computing and image processing. By using a basis that represents both location and spatial frequency, wavelets generalize Fourier transform. Directional wavelet transforms go further for 2D or 3D signals, by using basis functions that are also localized in orientation. From other directional wavelet transforms, a curvelet transform differs as such the degree of localization in orientation varies with scale. In particular, fine-scale basis functions are long ridges; the shape of the basis functions at scale $j$ is $2^{-j} \times 2^{-j/2}$ so the fine-scale bases are skinny ridges with a precisely determined orientation.

For representing images (or other functions) which are smooth apart from singularities along smooth curves, where the curves have bounded curvature, the curvelets are an appropriate basis. i.e. for images where objects in it have a minimum length scale. For cartoons, geometrical diagrams, and text this property holds. The edges such images contain appear increasingly straight when one zooms in on them. By defining higher resolution curvelets to be more elongated than the lower resolution ones, Curvelets take advantage of this property. However, natural images (photographs) do not have this property; they have detail at every scale. Therefore, it is preferable to use some sort of directional wavelet transforms for natural images, whose wavelets have the same aspect ratio at every scale.

When the image is of the right type, curvelets provide a representation that is considerably sparser than other wavelet transforms. This can be quantified by considering the best approximation of a geometrical test image that can be represented using only $n$ wavelets, and analysing the approximation error as a function of $n$. The squared error decreases only as $O(\frac{1}{\sqrt{n}})$ for a Fourier transform. For a wide variety of wavelet transforms, including both directional and non-directional variants, the squared error decreases as $O(\frac{1}{n})$. The extra assumption underlying the curvelet transform allows it to achieve $O((\log n)^2 / n^2)$.

For computing the curvelet transform of discrete data, efficient numerical algorithms exist. The computational cost of a curvelet transform is approximately 10–20 times that of an FFT, and has the same dependence of $O(n^2 \log n \cdot n^2 \log n)$ for an image of size $mn \times n$. 


2.1. From Classical Wavelet to curvelet Transform:

Although the DWTs has established an impressive reputation as a tool for mathematical analysis and signal processing, it has the disadvantage of poor directionality, which has undermined its usage in many applications. In recent years significant progress in development of directional wavelets has been made. To improve directional selectivity, complex wavelet is one way. However, the complex wavelet transform has not been widely used in the past, since it is difficult to design complex wavelets with perfect reconstruction properties and good filter characteristics. By essentially using tensor-product one-dimensional (1-D) wavelets, the 2-D complex wavelets are constructed. The directional selectivity provided by complex wavelets (six directions) is much better than that obtained by the classical DWTs (three directions), but is still limited.

In 1999, Candès and Donoho proposed an anisotropic geometric wavelet transform named ridgelet transform which is optimal at representing straight-line singularities. Unfortunately, global straight-line singularities are rarely observed in real applications. To analyze local line or curve singularities, a natural idea is to consider a partition of the image, and then to apply the ridgelet transform to the obtained subimages. This block ridgelet-based transform, which is named curvelet transform, was first proposed by Candès and Donoho in 2000. Apart from the blocking effects, however, the application of this so-called first-generation curvelet transform is limited because the geometry of ridgelets is itself unclear, as they are not true ridge functions in digital images. Later, a considerably simpler second-generation curvelet transform based on a frequency partition technique was proposed by same authors. A variant of the second-generation curvelet transform was proposed recently, to handle image boundaries by mirror extension (ME). Previous versions of the transform treated image boundaries by periodization. Here, the main modifications are to tile the discrete cosine domain instead of discrete Fourier domain and to adequately reorganize data. The computational complexity of the obtained algorithm and the standard curvelet transform are same. The second-generation curvelet transform has been shown to be a very efficient tool for many different applications in solving partial different equations (PDEs), image processing, seismic data exploration and fluid mechanics. In this survey, we will focus on this successful approach and show its numerical and theoretical aspects as well as the different applications of curvelets.

The strength of the curvelet approach is their ability to formulate strong theorems in approximation and operator theory, from the mathematical point of view. To represent curve-like edges the discrete curvelet transform is very efficient. However, the current curvelet systems still have two main drawbacks: 1) they are not optimal for sparse approximation of curve features beyond C2-singularities, and 2) the discrete curvelet transform is highly redundant. The currently available implementations of the discrete curvelet transform (see www.curvelet.org) aim to reduce the redundancy smartly. However, independently from the good theoretical results on N-term approximation by curvelets, the discrete curvelet transforms is not appropriate for image compression. The question of how to construct an orthogonal curvelet-like transform is still open. There have been several other developments of directional wavelet systems in recent years with the same goal, namely a better analysis and an optimal representation of directional features of signals in higher dimensions. None of these approaches has reached the same publicity as the curvelet transform. However, we want to mention shortly some of these developments and also describe their relationship to curvelets.
This feature is paid by high redundancy. Applications of Gabor wavelets focused on image classification and texture analysis. Gabor wavelets have also been used for modeling the receptive field profiles of cortical simple cells. Applications of Gabor wavelets suggested that the precision in resolution achieved through redundancy may be a relevant issue in brain modeling, and that orientation plays a key role in the primary visual cortex. The main differences between steerable wavelets/ Gabor wavelets and other X-lets is that the early methods do not allow for a different number of directions at each scale.

Contourlets, as proposed by Do and Vetterli, form a discrete filter bank structure that can deal effectively with piecewise smooth images with smooth contours. This discrete transform can be connected to curvelet-like structures in the continuous domain. Hence, the contourlet transform can be seen as a discrete form of a particular curvelet transform. Curvelet constructions require a rotation operation and correspond to a partition of the 2-D frequency plane based on polar coordinates; see the section “The Discrete Curvelet Frame.” This property is what makes the curvelet idea simple in the continuous case but causes problems in the implementation for discrete images. In particular, approaching critical sampling seems difficult in discretized constructions of curvelets. Critically sampling is easy to implement for contourlets. The directional filter bank, as a key component of contourlets, has a convenient tree-structure, where aliasing is allowed to exist and will be cancelled by carefully designed filters. The 3-D extensions of the 2-D contourlets are Surfacelets, that are obtained by a higher-dimensional directional filter bank and a multiscale pyramid. They can be used to efficiently capture and represent surface-like singularities in multidimensional volumetric data involving biomedical imaging, seismic imaging, video processing and computer vision. Surfacelets and the 3-D curvelets (see the section “Three-Dimensional Curvelet Transform”) aim at the same frequency partitioning, however, these two transforms achieve this goal with different approaches as we described above in the 2-D case..

### III. SINGULAR SPECTRAL ANALYSIS(SSA):

The singular spectrum analysis (SSA) is a nonparametric spectral estimation method in time series analysis. It combines the elements of classical time series analysis, multivariate statistics, multivariate geometry, dynamical systems and signal processing. SSA is a nonparametric method. It tries to overcome the problems of finite sample length and noisiness of sampled time series not by fitting an assumed model to the available series, but by using a data-adaptive basis set, instead of the fixed sine and cosine of the Blackman-Tukey method.

There are three basic steps in SSA: i) embedding the sampled time series in a vector space of dimension \( M \); ii) computing the \( M \times M \) lag-covariance matrix \( C_D \) of the data; and iii) diagonalizing \( C_D \).

**Step (i):** The time series \( \{ x(t) : t=1, \ldots, N \} \) is embedded into a vector space of dimension \( M \) by considering \( M \) lagged copies \( \{ x(t-j) : j=1, \ldots, M \} \) thereof. The choice of the dimension \( M \) is not obvious, but SSA is typically successful at analyzing periods in the range \((M/5, M)\).

**Step (ii):** One defines the \( M \times M \) lag-covariance matrix estimator \( C_D \). There are three distinct methods used widely to define \( C_D \). In the BK (Broomhead and King) algorithm, a window of length \( M \) is moved along the time series, producing a sequence of \( N' = N - M + 1 \) vectors in the embedding space. This sequence is used to obtain the \( N' \times M \) trajectory matrix \( D \), where the \( i \)-th row is the \( i \)-th view of the time series through the window. In this approach, \( C_D \) is defined by:
In the VG algorithm, $C_D$ is estimated directly from the data as a Toeplitz matrix with constant diagonals, i.e., its entries $C_{ij}$ depend only on the lag $|i-j|$: 

$$c_{ij} = \frac{1}{N-|i-j|} \sum_{t=1}^{N-|i-j|} x(t)x(t+|i-j|)$$

Burg covariance estimation is an iterative process based on fitting an AR model with a number of AR components equal to the SSA window length. Both the Burg and VG methods impose a Toeplitz structure upon the autocovariance matrix whereas the BK method does not. The Burg approach in principal should involve less "power leakage" due to the finite length of the time series and should therefore improve resolution. However, the Burg estimate can induce significant biases when nonstationarities and very low-frequency variations are present in the series. Thus in some cases to try the VG method will worth a while. Also, for long series ($N$ on the order of 5,000), the VG estimate is less computationally burdensome and thus is completed more quickly.

In practice, the VG method is more prone than is the Burg method to numerical instabilities (yielding negative eigenvalues) when pure oscillations are analyzed. The BK method is thus somewhat less prone to problems with nonstationary time series, although the VG method seems untroubled by all but the most extreme nonstationarities. However the Toeplitz methods do appear to yield more stable results under the influence of

Step (iii): The covariance matrix calculated from the $N$ sample points, is then diagonalized and the eigenvalues are ranked in decreasing order. The eigenvalue $\{\lambda_k, k=1,...,M\}$ gives the variance of the time series in the direction specified by the corresponding eigenvector $E_k$, the square roots of the eigenvalues are called singular values and the corresponding set the singular spectrum. These terms give SSA its name; BK showed how to obtain singular spectrum by SVD applied to the trajectory matrix $D$. VG called the $E_k$’s temporal empirical orthogonal functions (EOFs), by analogy with the meteorological term used when applying PCA in the spatial domain.

### 3.1. Principal of SSA:

SSA is a recent technique of time-series analysis and forecasting with multiple potential in different applications, going from market research or social science to data mining. With origin in the former Soviet Union during the 1980s, there are several related publications in the last 20 years, although some authors stand out [12], [13]. Here, the SSA concept and capabilities are briefly introduced, along with a complete mathematical description of the algorithm and a practical example for an easy understanding.
3.2. Concept
To decompose an original series into several independent components or subseries is the main objective of SSA. These components are interpretable, i.e., they can be mainly identified as varying trend, oscillations, or noise. Therefore, the main capabilities of SSA can be summarized as follows [12]:
1) extraction of trends, periodic components, and smoothing;
2) complex trends and periodicities with varying amplitudes;
3) finding structures in short time series;
4) envelopes of oscillating signals.
All these capabilities make SSA a really interesting approach, particularly as most research studies have not yet taken it into consideration in HSI.

3.4. Application of SSA
Given a particular sample, e.g., a spectral pixel in HSI, the SSA aims to achieve improved reconstruction of the pixel profile by means of the main eigenvalue components while abandoning the less representative or noisy components. Foreffective reconstruction of the original profile, there are two important parameters affecting the performance. The window size $L$ is the first parameter, which determines the total number of components that can be extracted in the decomposition stage. Taking $L = 10$, for example, ten eigenvalues are extracted, which leads to ten potential components generated. Obviously, the component corresponding to the first eigenvalue is much more significant than those corresponding to the following eigenvalues. The second parameter, i.e., eigenvalue grouping (EVG), denotes the selected combination of extracted components used for reconstruction. The use of only the first two components will remove most noise from the input data, for a data set with highly noisy content. However, if the noise level is low that only affects small components such as the ninth or the tenth, using just the first two components in the reconstructed signal may lead to loss of discriminating information in the samples.

IV. PROPOSED METHODOLOGY
The proposed denoising and feature extraction approach will be applied on hyperspectral images, and the flowchart is shown in Fig. 1 for reference. Hyperspectral sensors have a relatively high spectral resolution and can generate hundreds of observation channels. The obtained 3-D HSI data cube can be regarded as a stack of 2-D images of the same scene corresponding to different wavelengths, and the correlation between each two adjacent bands is fairly high.
In the proposed method, the first step is to perform the curvelet transform on each band of the hyperspectral image, and a few image stacks are generated after the transform as shown in Fig. 1. By applying the curvelet transform on each band, the band correlation property can be preserved so that SSA is able to exploit the spectral signature. To apply SSA in the spectral dimension for each detail image stack for feature extraction and denoising is the next step. After that, the denoised detail images at each band are gathered according to their original location, followed by the inverse curvelet transform to get the denoised hyperspectral image.

4.1 Applying SSA In The Curvelet Domain

In this paper, a hyperspectral image is denoted as $I(p, q) = (I_1(p, q), I_2(p, q), \ldots, I_B(p, q)) \in \mathbb{R}^B$, where $p \in [1,P]$, $q \in [1,Q]$, $P \times Q$ is the spatial dimension of the hyperspectral image, and $B$ is the number of bands. Represents the set of real numbers with the pixel intensity $I_b(p, q)$ at all sensor channels with $b \in [1,B]$. The 2-D curvelet transform via USFFT employed in this paper is completed using the toolbox CurveLab (version 2.1.2) [38]. Similar to the wavelet transform, the curvelet transform can also decompose the image into a coarse image and several detail images. Just like most image processing algorithms, the curvelet transform requires the processed image to be a square whose dimension is a power of 2. If the size of the original image is not a power of 2, pixels with a value of zero are padded to the next larger power of 2. Given the zero-padded HSI data set, $I_{pad}(m, n) = (I_{pad1}(m, n), I_{pad2}(m, n), \ldots, I_{padB}(m, n))$ where $m, n \in [1,N]$, consisting of $B$ bands where...
each band has N^2 pixels, the curvelet transform is performed on a band image I_{pad_b} to obtain the curvelet coefficients corresponding to that band c_{b}^D, i.e.,

\[ c_{b}^D = \text{CT}(I_{pad_b}) \]

where CT stands for the discrete curvelet transform operation explained in Section II. The decomposition results of the transform can be regarded as a superposition in the following form:

\[ c_{b,j}^D = c_{x,j} + \sum_{|n| \leq |j|} W_{b,n} \]

where \( c_{b,j} \) is the coarse version of the original band image with low-frequency contents, and \( W_{b,n} \) stands for the detail band image at scale \( 2^{-j} \) containing high-frequency contents. With an \( N \times N \) image, the default number of decomposition scales is \( J = \log_2(N) - 3 \) as set in the CurveLab toolbox. Take a band image with the size of 128 \( \times \) 128 for instance, the number of decomposition scales \( J \) will be four. According to the settings in the toolbox, there are eight orientations of the curvelet in the second and third scales, starting from the top-left wedge and increasing in a clockwise fashion, but for the coarsest and finest scales, there is only one direction. Thus,

\[ c_{b,j}^D = c_{b,1,1}^D + W_{b,1,1} + \sum_{j=2}^{J-1} \sum_{n=1}^{8} W_{b,n} \]

where \( W_{b,1,1} \) represents the finest scale with one orientation. The schematic of four decomposition scales corresponding to a 128 \( \times \) 128 image is shown in Fig. 2. Then, after applying the curvelet transform to all bands, there will be a coarse image stack and 17 detail image stacks.

Fig. 2. Illustration of a 128 \( \times \) 128 image with four decomposition scales. (a) First (finest) scale with one orientation. (b) Second scale with eight orientations. (c) Third scale with eight orientations. (d) Fourth (coarsest) scale with one orientation.

V. RESULTS

Fig 3 shows the Indian Pines data set which was collected in the Indian Pines test site in Northwest Indiana, USA on June 12, 1992. The scene consists of two-thirds agriculture, and one-third forest, or other natural perennial vegetation.
The above fig 5 shows the classification results of Indian pine data for the given original data. It is obtained by doing SVM classification.

Fig 5. SVM Classified image

Fig 6. Adaboost SVM output

Fig 6 shows adaboost svm output that avoids errors and get a more consistent result and obtain more accuracy.

mean class-by-class and average and overall accuracy values (%) of ten repeated experiments on testing samples of the original indian pine data set and ssa, ct-ssa, adaboost-ct-, followed by the standard deviation.
<table>
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<th>Class</th>
<th>SSA</th>
<th>CT-SSA</th>
<th>ADABOOST-CTSSA</th>
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<td>87.0385</td>
<td>90.4600</td>
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<tr>
<td>2</td>
<td>88.9185</td>
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<td>93.7500</td>
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</table>

Accuracy: (predicted class label) / (actual class label)

Since the proposed methodology is inspired by the feature extraction approach based on SSA, the proposed approach is denoted as CT-SSA, and other inspirational approaches are named SSA. The proposed CT-SSA approach actually belongs to the 1-D spectral processing technique for hyperspectral images. The testing is performed on different classes and the accuracy is been calculated. The accuracy is compared between SSA, CT-SSA and Adaboost-CT-SSA. Adaboost-CT-SSA is obtained good state of accuracy compared to SSA and CT SSA. When compared with only SSA, CT-SSA has better performance. It can be seen that those dimensionality reduction techniques only give comparable results compared with the original dataset, although they could speed up the classification process. Highest classification OA and AA achieved by Adaboost-CT-SSA.

VI. CONCLUSION

In this paper, two powerful tools, i.e., SSA and the curvelet transform, are combined for HSI feature extraction. By applying SSA in the curvelet domain, noise can be smoothed from the decomposed signals, resulting in more effective feature extraction. Inspired by applying PCA in the curvelet domain and another method of solely applying SSA on HSI data, the proposed method adaboost technology takes advantage of those approaches. By
using this adaboost technology the feature extraction made more accurate and the noise smoothen is high compared to other techniques.

REFERENCES


